Extended Abstract: Searching with Consistent Prioritization for Multi-Agent Path Finding[*]

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Abstract

This is an extended abstract of a previously published paper at AAAI 2019 (Ma et al. 2019). We generalize prioritized planning for Multi-Agent Path Finding from planning with a fixed total priority ordering of all agents to planning with all possible partial priority orderings. We present new theoretical results on its limitations in terms of completeness and optimality. We also present a novel prioritized algorithmic framework and demonstrate state-of-the-art solution qualities and success rates, often with runtimes similar to those of existing prioritized algorithms.

Introduction

In Multi-Agent Path Finding (MAPF) (Ma and Koenig 2017), we are given a connected undirected graph $G = (V, E)$ and M agents $\{a_i \mid i \in [M]\}$ ($[M] = \{1, \ldots, M\}$). Each a_i is given a unique start vertex $s_i \in V$ and a unique target vertex $t_i \in V$ and either moves to an adjacent vertex or waits at the same vertex at each discrete time $t = 0, \ldots, \infty$. Let $\pi_i(t)$ denote the vertex occupied by a_i at t. A *plan* consists of a set of paths, one path $\pi_i = \langle \pi_i(0), \ldots, \pi_i(T_i), \pi_i(T_i + 1), \ldots \rangle$ for each a_i, where $\pi_i(0) = s_i$ and $\pi_i(t) = t_i$ for all times $t = T_i, \ldots, \infty$. The *arrival time* T_i of agent a_i at t_i is the earliest time when it has reached t_i and stops moving. A *vertex collision* is a tuple $\langle a_i, a_j, v, t \rangle$ where a_i and a_j occupy the same v at the same t. An *edge collision* is a tuple $\langle a_i, a_j, u, v, t \rangle$ where a_i and a_j traverse $(u, v) \in E$ in opposite directions at the same t. A solution is a plan that consists of collision-free paths for all agents. Its quality is measured by the *flowtime* $\sum_{i \in [M]} T_i$, the sum of the arrival times of all agents.

MAPF arises in many applications, such as for aircraft-towing vehicles (Morris et al. 2016), warehouse and office robots (Wurman, D'Andrea, and Mountz 2008; Veloso et al.

2015), game characters (Ma et al. 2017b), and other multi-agent systems (Ma et al. 2017a). MAPF is NP-hard to solve optimally (Yu and LaValle 2013b; Ma et al. 2016b) and can be solved with reductions to other well-studied combinatorial problems (Surynek 2015; Yu and LaValle 2013a; Erdem et al. 2013) and dedicated MAPF algorithms (Standley and Korf 2011; Luna and Bekris 2011; Goldenberg et al. 2014; Sharon et al. 2013; Wagner and Choset 2015; Sharon et al. 2015), as described in several surveys (Ma et al. 2016a; Felner et al. 2017).

Prioritized MAPF algorithms (Silver 2005; Sturtevant and Buro 2006) use the following simple prioritized-planning scheme (Erdmann and Lozano-Pérez 1987): Each a_i is given a unique priority and computes, in priority order, a minimum-cost path from s_i to t_i that avoids collisions with the (already planned) paths of all agents with higher priorities. Existing (standard) prioritized MAPF algorithms are often used as parts of MAPF solvers (Velagapudi, Sycara, and Scerri 2010; Wang and Botea 2011; Cáp, Vokrínek, and Kleiner 2015). However, they use a predefined total priority ordering of the agents and can thus result in solutions of bad quality or even fail to find any solutions for solvable MAPF instances, where a different total priority ordering could have resulted in solutions of higher quality. In this paper, we thus consider a generalized form of prioritized planning with all possible total priority orderings. We discuss the limitations of prioritized planning. We also develop two prioritized MAPF algorithms, Conflict-Based Search with Priorities (CBSw/P) and Priority-Based Search (PBS), that systematically explore "good" priority orderings.

Theoretical Results

We summarize the theoretical results: (1) Some MAPF instances that are solvable are not solvable with prioritized planning. (2) Some MAPF instances that are solvable with prioritized planning are only solvable with prioritized planning for a single total priority ordering. (3) Some MAPF instances that are solvable with prioritized planning are not optimally solvable with prioritized planning for any total priority ordering. (4) Even worse, some MAPF instances that are optimally solvable with prioritized planning require prioritized planning not only to use the correct total priority ordering but also break ties correctly when planning paths for the agents, which—if done incorrectly—can prevent priori-

tized planning from finding any solution. We refer the reader to the original paper (Ma et al. 2019) for the detailed theorems and proofs.

Algorithms

Conflict-Based Search with Priorities (CBSw/P) is an adaptation of Conflict-Based Search (CBS) (Sharon et al. 2015) to prioritized planning. It explores the space of all total priority orderings lazily using a systematic best-first search: It introduces an ordered pair of agents only when their paths collide. Priority-Based Search (PBS) explores the space of all total priority orderings lazily using a systematic depth-first search: It takes a user-specified partial priority ordering as input, dynamically adds new ordered pairs of agents to it, and plans paths that are consistent with the resulting partial priority ordering. Standard prioritized MAPF algorithms are special cases of PBS.

We compare CBSw/P and PBS to a state-of-the-art implementation of CBS (Felner et al. 2018) and several PBS variants that simulate standard prioritized MAPF algorithms with different total priority orderings on a 2.50 GHz Intel Core i5-2450M laptop with 6 GB RAM. We find that CBSw/P often computes optimal or near-optimal solutions and is more efficient than CBS. PBS also computes near-optimal solutions and is much more efficient than CBSw/P. Moreover, PBS finds solutions for many MAPF instances where standard prioritized MAPF algorithms cannot and solves MAPF instances with six hundred agents on a video game map in 35.18 seconds on average.

We refer the reader to the original paper (Ma et al. 2019) for a detailed description and theoretical analysis of CBSw/P and PBS and more experimental insights.

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