Evaluation of the interfacial shear strength and residual stress of TiAlN coating on ZIRLO™ fuel cladding using a modified shear-lag model approach

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Abstract

This paper investigates the residual stresses and interfacial shear strength of a TiAlN coating on Zr–Nb–Sn–Fe alloy (ZIRLO™) substrate designed to improve corrosion resistance of fuel cladding used in water-cooled nuclear reactors, both during normal and exceptional conditions, e.g., a loss of coolant event (LOCA). The distribution and maximum value of the interfacial shear strength has been estimated using a modified shear-lag model. The parameters critical to this analysis were determined experimentally. From these input parameters the interfacial shear strength between the TiAlN coating and ZIRLO™ substrate was inferred to be around 120 MPa. It is worth noting that the apparent strength of the coating is high (~3.4 GPa). However, this is predominantly due to the large compressive residual stress (3 GPa in compression), which must be overcome for the coating to fail in tension, which happens at a load just 150 MPa in excess of this.

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1. Introduction

Zirconium alloys are commonly used as the fuel cladding for water cooled nuclear fission reactors, mainly due to their low neutron cross-section, good corrosion resistance during normal operating conditions and sufficient mechanical strength [1]. Despite high corrosion resistance at normal operating temperatures (around 300 °C) [2], Zr alloys oxidise very rapidly when exposed to temperatures a few hundred degrees higher. This is an exothermic reaction, which can further accelerate oxidation and, at temperatures beyond 1000 °C, potentially lead to disintegration of the fuel rods, as highlighted during the Fukushima Daiichi nuclear accident. For this reason new research activities have been initiated worldwide to develop accident tolerant fuels (ATF). Additionally, ATFs could also provide further enhancements in corrosion performance during normal operating conditions enabling the development of fuel assemblies for very high burn-up.

One concept for ATF is to coat the outside of current zirconium tubes with material that has an inherently high temperature oxidation resistance. Refractory metal nitride compounds, such as TiAlN, have been proposed as promising contenders for coatings on Zr for ATF applications [3,4]. The principle idea of TiAlN coating is that during exposure to very high temperatures, aluminium diffuses to the surface and reacts with oxygen to form a thin protective oxidation barrier. This significantly improves oxidation performance of the system, as oxygen diffusion through aluminium oxide is several orders of magnitude lower than through zirconium oxide.

However, during service, the fuel cladding displays dimensional instability as a result of irradiation enhanced creep and irradiation induced growth [5–7]. Therefore, an important aspect of coated cladding material is the structural integrity of the system, particularly the coating fracture behaviour, residual stresses in the coating and bond strength between the coating and the zirconium substrate. One common approach for analysing the fracture and adhesion behaviour between a brittle coating and a ductile substrate is to employ a model based on the shear-lag approximation [8–12] to predict the transfer of load between substrate and coating. Here, uniaxial tensile loading experiments are used to introduce parallel cracks transverse to the straining direction...
(transverse cracks) in the coating. Providing the initial residual stress in the coating is taken into account, the fracture strength of the coating can be estimated from the strain attained when the transverse cracks first start to appear. Subsequently, the interfacial shear strength can be evaluated by measuring the crack spacing (either the maximum, minimum or average spacing), achieved on further straining to the point at which the transverse crack frequency in the coating saturates. To infer the interfacial strength the model proposed by Agrawal and Raj (A-R model) has been used extensively [8,13]. It has been proven effective for many systems having a brittle coating adhered to a ductile substrate [11,13–17]. However, the model assumes that the shear stress is a sine wave having a wavelength equal to the fragment length (i.e. zero at the ends and the mid-point of the fragment), which is not physically based and is unlikely to be the case [9–11].

A modified shear-lag model is used in this paper, aiming to provide an approach, which is both easy to deploy and accurately represents the distribution of the interfacial shear stress (ISS) for a wide range of coating-substrate systems. It requires a knowledge of the coating residual stresses, which was determined by laboratory-based X-ray diffraction (XRD) and Raman spectroscopy. The model was employed to infer the ISS between the TiAlN on a ZIRLO™ substrate. In addition, key input parameters associated with the proposed model were measured experimentally.

The assessment of residual stresses in the coating and bond strength between the coating and the substrate aims to provide a guideline in an effort to develop TiAlN coatings for applications such as ATF.

2. Model formulation

A model based on the shear-lag approximation [18] for fibre/matrix composites systems has been developed in this work for the evaluation of the interfacial shear strength and is applicable not only for the TiAlN/ZIRLO™ structure, as discussed in this paper, but for a wide range of brittle coating/ductile substrate systems.

Under increasing tensile loading, a brittle coating eventually cracks before the substrate undergoes plastic deformation. A schematic of the cross-section of a fragmented region of the coating between two cracks, detailing key parameters used in the analysis, is given in Fig. 1. For the following shear-lag analysis, the origin of the coordinate system is located centrally at the top of this fragmented coating where the length of the segment is $Z$, from $-Z$ to $Z$ and the coating thickness is $b$.

Fig. 1(a) displays $z$ axis is parallel to the coating/substrate interface, whereas $l$ axis is perpendicular to the interface from the origin into the substrate. Fig. 1 (b) shows that when the coating is loaded to fracture, the stress variation $\tau$ in the substrate at given distance $z$ away from the fragment central along $z$ axis, is obtained by balancing the shear force by a neighbouring stress pair $\tau_1$ ($l_1$ away from the interface) and $\tau_2$ ($l_2$ away from the interface) over length $dz$.

$$ l_1 \cdot \tau_1 \cdot dz = l_2 \cdot \tau_2 \cdot dz $$

(1)

$$ \frac{\tau_1}{\tau_2} = \frac{l_2}{l_1} $$

(2)

$$ \tau_1 = \left( \frac{l_1}{l_2} \right) \cdot \tau_L $$

(3)

where $\tau_1$ and $\tau_2$ are neighbouring shear stress; $l_1$ and $l_2$ are distances away from the coating/substrate interface; $dz$ is the length of the fragment over which the neighbouring shear force $\tau_1$ and $\tau_2$ are balanced, as shown in Fig. 1: $\tau_1$ is the shear stress at the interface between the coating and substrate, and $\delta$ is the coating thickness. $L$ represents a large distance (far-field) into the substrate where the shear stress does not change with the depth parameter $l$.

The definition of shear strain gives

$$ \gamma = \frac{du}{dl} = \frac{\tau_L}{G_s} \frac{\delta}{L} $$

(4)

$$ U_L - U_b = \frac{\tau_1 \cdot \delta}{G_s} \ln \left( \frac{L}{\delta} \right) $$

(6)

$$ \tau_1 = \frac{G_s}{\delta \cdot \ln \left( \frac{L}{\delta} \right)} \cdot (U_L - U_b) $$

(7)

where $U_L$ is the far-field strain and $U_b$ is the strain at coating/substrate interface, and $G_s$ is the shear modulus of the substrate.

The term $\ln \left( \frac{L}{\delta} \right)$ is not very sensitive to the ratio of $L$ over $\delta$, as it is in the logarithmic term. It is therefore possible to assume $L$ to be the substrate thickness in most cases (when $L$ is still comparable to $\delta$).

Equation (7) provides the expression of interfacial shear strength $\tau_1$ as a function of the mismatch between far-field strain $U_L$ and interfacial strain $U_b$.

The build-up of the in-plane tensile stress $\sigma_t$ is related to the distribution of interfacial shear stress $\tau$, force balance of the thin coating itself requires,
\[ \tau_i \cdot dz = -\delta \cdot d\sigma_c \]

where \( \sigma_c \) is the in-plane stress within the thin coating.

Combining Equation (8) and Equation (7) gives

\[ \frac{d\sigma_c}{dz} = \frac{\tau_i}{\delta} = \frac{G_s \cdot (U_L - U_B)}{r^2 \ln \left( \frac{L}{h} \right)} \]

Expressing \( G_s \) in terms of the substrate Young’s modulus \( E_c \) and Poisson’s ratio \( \nu_s \) gives

\[ \frac{d\sigma_c}{dz} = \frac{E_s}{(1 + \nu_s)} \frac{(U_L - U_B)}{r^2 \ln \left( \frac{L}{h} \right)} \]

At the coating interface,

\[ \left. \frac{du}{dz} \right|_{z=0} = \epsilon_c = \frac{\sigma_c}{E_c} \]

In the substrate far-field,

\[ \left. \frac{du}{dz} \right|_{z=L} = \epsilon_s \]

where \( \epsilon_c \) is the coating strain and \( \epsilon_s \) is the substrate strain far-field.

Differentiating Equation (10) gives,

\[ \frac{d^2\sigma_c}{dz^2} = \frac{E_s}{(1 + \nu_s) \cdot r^2 \ln \left( \frac{L}{h} \right)} \left( \epsilon_s - \frac{\sigma_c}{E_c} \right) \]

\[ \frac{d^2\sigma_c}{dz^2} = \frac{n^2 \cdot (\sigma_c - E_c \cdot \epsilon_s)}{\ln \left( \frac{L}{h} \right)} \]

where \( n = \sqrt{\frac{E_c \cdot \epsilon_s}{\ln \left( \frac{L}{h} \right) \cdot E_c}} \).

Solving Equation (14) gives

\[ \sigma_c = E_c \cdot \epsilon_s + B \cdot \sinh \left( \frac{nZ}{\delta} \right) + D \cdot \cosh \left( \frac{nZ}{\delta} \right) \]

On applying the boundary conditions \( \sigma_c \) at \( z = \pm Z \);

\[ B = 0; \quad D = -E_c \cdot \epsilon_s \cdot \sech \left( \frac{nZ}{\delta} \right) \]

\[ \sigma_c = E_c \cdot \epsilon_s \cdot \left[ 1 - \sinh \left( \frac{nZ}{\delta} \right) \cdot \cosh \left( \frac{nZ}{\delta} \right) \right] \]

Combining Equation (17) with Equation (8) gives,

\[ \tau_i = -\delta \cdot \frac{d\sigma_c}{dz} = n \cdot E_c \cdot \epsilon_s \cdot \sinh \left( \frac{nZ}{\delta} \right) \cdot \sech \left( \frac{nZ}{\delta} \right) \]

Equation (17) and Equation (18) describe the distribution of the in-plane coating stress \( \sigma_c \) as a function of distance \( z \). It is demonstrated from Equation (17) and Equation (18) that the maximum in-plane stress \( \sigma_c \) peaks at the centre of the fragment whereas the interfacial shear stress is peaked at the ends of the fragment (where the cracks are). On applying boundary conditions of \( \tau_i = \tau_{\text{imax}} \) when \( z = \pm Z \) into Equation (18) gives

\[ |\tau_{\text{imax}}| = \frac{n \cdot E_c \cdot \epsilon_s}{\coth \left( \frac{nZ}{\delta} \right)} \]

with

\[ \epsilon_s = \frac{\coth \left( \frac{nZ}{\delta} \right) \cdot |\tau_{\text{imax}}|}{n \cdot E_c} \]

When the peak coating stress in the centre of the fragment reaches the coating fracture strength \( \sigma_c \) the fragment cracks into two. With increased loading of the substrate this process repeats itself resulting in further fragmentation until the number of cracks saturate. This occurs when the remaining fragments are too short to reach the critical fracture stress.

At this saturated cracking level, Equation (17) gives

\[ \sigma_f = E_c \cdot \epsilon_s \cdot \left[ 1 - \sech \left( \frac{nZ}{\delta} \right) \right] \]

Combining Eq. (21) with Eq. (20) gives

\[ |\tau_{\text{imax}}| = \frac{\sigma_f}{n \cdot \coth \left( \frac{nZ}{\delta} \right) \cdot \coth \left( \frac{nZ}{\delta} \right)} \]

\[ \sigma_f = \sigma_a + \sigma_r = E_c \cdot \epsilon_{cf} + \sigma_r \]

where \( \sigma_a \) is the stress in the coating from the applied load \( (\sigma_a = E_c \cdot \epsilon_{cf}) \) and \( \sigma_r \) is the residual stress. The term \( \epsilon_{cf} \) is the strain during loading at which cracks first appear.

By combining Equation (23) with Equation (24),

\[ |\tau_{\text{imax}}| = \frac{E_c \cdot \epsilon_{cf} + \sigma_r}{n \cdot \coth \left( \frac{nZ}{\delta} \right) \cdot \coth \left( \frac{nZ}{\delta} \right)} \]

If the fragment is slightly longer than the critical length for fracture, it will fracture into two halves while if it is slightly shorter than the critical length it cannot. Hence, at saturation one would expect a distribution of fracture lengths between the critical length and a half the critical length. Based on an ideal normal distribution, the half crack distance \( Z \) in Equation (25) is approximately \( 2 / 3Z \), where \( Z \) is the average crack spacing at saturated level after tensile testing.

\[ |\tau_{\text{imax}}| = \frac{E_c \cdot \epsilon_{cf} + \sigma_f}{n \cdot \coth \left( \frac{2 \cdot nZ}{3} \right) \cdot \cosh \left( \frac{2 \cdot nZ}{3} \right)} \]

with \( n \) expressed previously as

\[ n = \sqrt{\frac{E_c}{(1 + \nu_s) \ln \left( \frac{L}{h} \right) \cdot E_c}} \]
Equation (26) provides an expression of the maximum interfacial shear stress with measurable parameters. The utilisation of this method is shown below with the example of interfacial shear strength calculation between TiAlN coating and zirconium alloy substrate.

A summary of each parameter and the corresponding method of measurement is given below in Table 1.

3. Experimental methods

3.1. Deposition process

A ~10 μm thick TiAlN coating was deposited onto a ~1000 μm zirconium alloy substrate (ZIRLO™) using a cathodic arc physical vapour deposition (CAPVD) method. Cathodic arc falls into the classification of Physical Vapour Deposition (PVD) coating techniques. The term PVD denotes those vacuum deposition processes where the coating material is evaporated or removed by various mechanisms (resistant heating, ablation, high-energy ionized gas bombardment, or electron gun), and the vapour phase is transported to the substrate forming a coating. PVD is often classified as a "line-of-sight" process in which evaporated atoms travel from the source material to the substrate in a straight path. The residual stresses in the PVD coating are generally compressive due to coating bombardment onto the substrate, but can be controlled depending on the deposition parameters. These compressive stresses are often beneficial as they retard the formation and propagation of cracks in the coating. PVD coating processes generally take place between temperatures of 200 °C–500 °C to minimize stresses associated with thermal expansion mismatch as compared to the high temperatures (1000 °C) of chemical vapour deposition CVD.

In the cathodic arc deposition process, a pulsed or continuous high current-density, low voltage electric current is passed between two separate electrodes (cathode and anode) under low pressure vacuum, vaporizing the cathode material while simultaneously ionizing the vapour, forming a plasma. The high current density (usually 10³–10⁶ A/cm²) causes arc erosion by vaporisation and melting while ejecting molten solid particles from the cathode surface, with a high percentage of the vapourised species being ionised with elevated energy (50–150 eV) and multiply charged.

For example, in the case of TiAIN, as the vaporised titanium-aluminium (cathode target) passes through the arc, it becomes ionised forming plasma. The plasma is directed towards the substrate's surface, and in the presence of nitrogen, forms a TiAIN coating. The kinetic energy of the depositing species in cahotic arc, are much greater than those of other PVD processes with energies between 50 and 150 eV. Therefore, the plasma becomes highly reactive as a greater percentage of the vapour is ionized. In addition, the cathodic arc process allows tailoring of the interfacial products, especially in multilayer coatings, and does not produce a distinct coating/substrate interface, which may be undesirable. As a result of the high kinetic energy, an intermixed layer of the substrate and coating or between layers of a multilayer coating (1–30 nm thick) can be formed that increases the degree of coating adhesion while minimizing residual stresses.

The main disadvantage of cathodic arc deposition is that it produces macroparticles of metals and liquid droplets that are the result of intense, localized heating from the arc. This heating produces small amounts of liquid metal that become entrapped within the depositing coating and serve as stress concentrations and crack initiation sights. To decrease the number of molten macroparticles, filtered cathodic arc systems are often used. An electromagnet field is applied, and due to momentum, the larger macroparticles do not deposit on the substrate surface as they get filtered away from the substrate. In general, filtered arc deposition usually has a lower deposition rate than unfiltered. In addition, target efficiency can be increased by steering the arc across the cathode surface. A magnetic field is applied that steers the arc across the surface of the targets and thus reduces the dwell time (localized heating) at any given point.

In the present case, diffraction pattern recorded on the coating suggests that it is Ti₆₆₅Al₃₅N (ICDD 04-017-5094). The crystal structure is a cubic rock salt type with the Ti and Al atoms occupying the FCC positions and N sitting interstitially.

3.2. Measurement of bulk elastic properties

Nanoindentation has been established as an effective tool to measure the bulk elastic properties [19]. For such elastic modulus measurements, the coated sample was cut and mounted in cross-section, which was ground and polished with colloidal silica OPS. For the indentation experiments, a MTS Nanoindenter XP (Agilent Technologies) was employed. The position of the coating layer was defined using the nanovision stage based on the variation in topography arising from the polishing process. The sample was held on a pneumatic-vibration-isolation table, which was enclosed in a cabinet to ensure thermal stability. Indentation was carried out using the Dynamic Contact Module (DCM II) equipped with a Berkovich triangular-diamond pyramid tip. The indent depth was set at 200 nm and 20 indents, located along the centreline of the coating, were recorded for the elastic modulus measurements. The Poisson’s ratios were taken from literature with 0.23 for TiAIN [20] and 0.34 for ZIRLO™ [2].

3.3. In-situ loading in SEM

In-situ loading using a Kammrath & Weiss micro-tensile-testing device was conducted in a FEI Quanta 650 field emission gun scanning electron microscope (FEGSEM), operating at an accelerating voltage of 20 kV in backscattered electron imaging (BSE) mode.

One purpose of this in-SEM loading experiment was to obtain the fracture (maximum elastic) strain of the TiAIN coating by analysing the images recorded during mechanical loading using digital image correlation. Specimens were strained in increments of 0.05% using a crosshead speed of 5.0 μm/s. A BSE image of the central gauge region of the specimen was taken after each strain increment. Once the first crack was observed, the step size was increased to 0.1% at the same strain rate in order to determine the saturated crack spacing. Each image was taken at a fixed magnification and 5 tensile samples were measured to get statically valid date results.

A systematic measurement of the crack spacing data at each strain level was conducted using Image® image analysis software using a standard line intercept method [16].

3.4. X-ray diffraction sin²ψ method for residual stress analysis

Residual stresses in the coating were determined initially by using the sin²ψ method on a Bruker Discover D8 (Cu tube X-ray
source). A Ni k-β filter together with a polycapillary was applied to ensure a parallel beam configuration. Alignment was confirmed by analysing a standard corundum sample with known peak positions. The fundamental equation relating stress and strain for a rotationally symmetric biaxial stress state is [21]:

$$\frac{d_\Psi - d_0}{d_0} = 1/2\sqrt{2} \sigma_{||} \sin^2 \Psi + 2\sqrt{2} \sigma_{\perp}$$  \hspace{1cm} (27)$$

where $d_\Psi$ is the d-spacing measured at a particular tilt angle, $\Psi$, $d_0$ is the stress free lattice parameter, $1/2\sqrt{2}$ and $2\sqrt{2}$ are diffraction elastic constants and $\sigma_{||}$ is the residual stress. Differentiating with respect to $\sin^2 \Psi$ gives:

$$\frac{\partial d_\Psi}{\partial \sin^2 \Psi} = \frac{1}{2\sqrt{2}} \sigma_{||} \sin^2 \Psi$$  \hspace{1cm} (28)$$

From this equation it follows that a plot of d-spacing v.s. $\sin^2 \Psi$ should be linear with a gradient proportional to the residual stress. $d_0$ can be determined by interpolation of the d-spacing v.s. $\sin^2 \Psi$ data to the strain free direction of the biaxial stress state, $\Psi^\ast_{hlh}$ [21]:

$$\Psi^\ast_{hlh} = \sin^{-1} \sqrt{-\frac{2\sqrt{2}}{1/2\sqrt{2}} \sin^2 \Psi}$$  \hspace{1cm} (29)$$

The diffraction elastic constants, $1/2\sqrt{2}$ and $2\sqrt{2}$, were inferred from single crystal elastic constants for TiAIN ($C_{11} = 447$, $C_{12} = 158$, $C_{44} = 203$ [22]) using the Kröner model via the software IsoDEC [23].

Residual stress in the sample was determined from 3 different diffraction peaks (200, 311 and 222), by independently analysing the d v.s. $\sin^2 \Psi$ behaviour of the individual reflections. Scans were conducted in $\psi$ mode (i.e. the sample is tilted in a plane perpendicular to that containing the source and detector).

The 200 peak was not overlapped by substrate peaks, which leant itself to a straightforward analysis of stress using a standard symmetric geometry (i.e. the angle between the X-ray beam and sample surface is half of 20). For the analysis of diffraction peaks in this geometry, data was firstly background corrected, before an absorption, $A_{20h}$, (Eq. (30)) [21] and Lorentz polarisation, $L_p$, (Eq. (31)) [21] correction.

$$A_{20h} = \left(1 - \exp\left(-\frac{2\mu t}{\sin \theta}\right)\right)$$  \hspace{1cm} (30)$$

$$L_p = \frac{1}{2} \frac{1 + \cos^2 \theta}{\sin \theta} \frac{1}{2} \sin 2 \theta$$  \hspace{1cm} (31)$$

where $\mu$ is the linear absorption coefficient (0.0574 $\mu$m$^{-1}$), $t$ the coating thickness and $\theta$ the diffraction angle. After correction, peaks were fitted using a PearsonVII function to determine the peak centres.

Conversely, the 311 and 222 peaks were severely overlapped with reflections from the substrate. Therefore, an asymmetric diffraction geometry was needed to lower the X-ray penetration and to limit the influence of the underlying Zr peaks. It was found that an incident angle of 10° (between the source and the sample surface) would lower the intensity of the Zr peaks (at $\psi = 0$) to a level where they were no longer significant. The intensity of the 0114 Zr peak, with different incident angles, was monitored to determine this.

In an asymmetric diffraction configuration a constant incident angle, of 10° in this case, is used for all $\psi$ tilts. The sample tilts with this geometry no longer correspond with those in the symmetric 0–20 geometry. A coordinate transformation is therefore needed [24]:

$$\cos \psi = \cos (\theta - \alpha) \cos \psi_d$$  \hspace{1cm} (32)$$

where $\psi_d$ is the tilt angle of the diffractometer and $\Psi$ is then the tilt angle corresponding to that in 0–20 geometry. Again the diffraction profiles were absorption, $A_a$, and Lorentz polarization, $L_p$, corrected [24]:

$$A_a = \frac{\sin \omega_2}{\sin \omega_1 + \sin \omega_2} \left(1 - e^{-\mu t \left(\frac{1}{\sin \gamma} + \frac{1}{\sin \gamma_d}\right)}\right)$$  \hspace{1cm} (33)$$

with:

$$\omega_1 = 90° - \arctan \sqrt{\frac{1}{\cos^2 \psi_d \tan^2 \alpha} + \tan^2 \psi_d}$$  \hspace{1cm} (34)$$

$$\omega_2 = 90° - \arctan \sqrt{\frac{1}{\cos^2 \psi \tan^2 (2\theta - \alpha)} + \tan^2 \psi_d}$$  \hspace{1cm} (35)$$

where $\alpha$ is the X-ray incidence angle.

$$L_p = \frac{1 + \cos^2 2\theta}{\sin^2 \theta}$$  \hspace{1cm} (36)$$

The peak position is also affected by refraction and the peak position within the material, $2\theta'_\psi$, is given by:

$$\tan (2\theta'_\psi) = \tan (2\theta_\psi - \alpha) + \tan \alpha$$  \hspace{1cm} (37)$$

where:

$$\tan \psi'_d = \frac{\tan \psi_d}{\tan \gamma} \tan \psi_d$$  \hspace{1cm} (38)$$

$$\tan \alpha' = \tan \alpha \frac{\sin \psi_d}{\sin \psi'_d}$$  \hspace{1cm} (39)$$

$$\sin \gamma' = n \sin \gamma$$  \hspace{1cm} (40)$$

$$\gamma = 90° - \omega_1$$  \hspace{1cm} (41)$$

and $n$ is the refraction coefficient (for TiN, $n = 0.9999845$ [24]).

In addition to single peak analyses, residual stresses were also determined by studying whole diffraction patterns at a number of $\psi$ angles. Rietveld analyses were conducted to determine the lattice parameter at each $\psi$ angle. A plot of lattice parameter, $a$, against $\sin^2 \Psi$ was produced and residual stresses calculated according to Eq. (28), but with the d-spacing of the individual reflection replaced with the lattice parameter. By using this method the hkl dependence is lost and therefore bulk elastic constants can be used instead of diffraction elastic constants. Bulk constants can be measured more easily and indeed have been obtained experimentally in this work using nano-indentation. This technique also limits any issues related to plasticity, which can cause diffraction peaks to display non-linear strain behaviour with stress.

For the Rietveld analysis, diffraction patterns were obtained in symmetric diffraction geometry. While this geometry created some overlapping of substrate and coating reflections, it did not pose a problem to obtain reliable data as the Rietveld method uses the whole diffraction pattern rather than an individual peak [25].
3.5. Micro-Raman spectroscopy for residual stress analysis

In addition to XRD based residual stress analysis, residual stresses of the coating were estimated by employing a micro-Raman spectrometer (Renishaw-2000) with green laser light (wavelength of 633 nm) and a spot size of ~2 µm. The spectral resolution of the spectrometer was 1 cm⁻¹, and a depth in the coating of around 1–2 µm is sampled.

Before testing, the Raman spectroscopy was calibrated using a silicon (Si) single-crystal sample using the characteristic Si peak at a wavenumber of 520 cm⁻¹. Raman peaks were fitted using the Gaussian peak fitting function provided by commercial software Origin®. The standard deviation for the characteristic Si peak shift was ±0.1 cm⁻¹ giving a stress resolution of ±0.1 GPa.

In order to calibrate the behaviour of the Raman peak shift with stress (i.e. to get a peak shift per increment of stress value) a series of known uniaxial loads were applied to the sample using a Kammrath & Weiss micro-tensile-testing device while determining the Raman peak position. The laser spot was positioned at the centre of the analytical area. Images and Raman spectra were obtained using a light optical microscope with a ×50 (numerical aperture = 0.75) objective lens, before and after each load step during the in-situ loading experiment, without laser light polarisation. Note that the gauge length of the tensile specimen was approximately 30 mm. At each loading step, a difference in peak position of less than 0.1 cm⁻¹ (equivalent to 56 MPa) was found across multiple locations. Raman measurements were undertaken at four different load levels for calibration purposes. Subsequently, the same loading experiments were repeated in a SEM in order to obtain the corresponding strain levels through digital image analysis. The strain was subsequently converted to stress using the Young’s modulus of the coating, which had been determined by nano-indentation (Section 3.2).

Additionally, a stress-free Raman peak position value is needed before the residual stress in the coating can be determined. This was obtained by further loading the sample to induce cracks in the coating. The sample was subsequently unloaded and Raman measurements were undertaken at multiple locations at the fragment ends near the crack. The crack provides an additional free surface and therefore the stress is zero at the ends of coating fragments near the crack. The average stress free TiAlN peak position was located at 249.6 cm⁻¹, which is similar to the literature values for stress-free TiAlN [26].

Following [19], the stresses can finally be estimated from the Raman characteristic peak shift through the following equation:

\[ \sigma = \frac{\Delta v}{\Pi u} \]  

(42)

where \( \Delta v \) is the Raman peak shift (cm⁻¹), and \( \Pi u \) is the uniaxial piezospectroscopic coefficient (cm⁻¹/GPa), which was calibrated experimentally in this work.

4. Experimental results

4.1. Coating thickness and elastic constants

In order to evaluate the interfacial shear strength precisely the aim was to measure the parameters in Equation (26) with high accuracy.

Firstly, the coating thickness was measured with SEM cross-sectional images at multiple locations. Average coating thickness was observed at ~8 µm.

The modulus of the TiAlN coating was determined from 20 nanoindents to be 406.5 GPa ± 5.3 GPa. The lateral extent (500 nm) of each indent was optimised to reduce any influence from either the substrate or the resin material. Measurements near the edges were excluded as a reduction in modulus was observed close to the coating surface.

Similarly, the Young’s modulus of the ZIRLO™ substrate \( (E_y) \) was measured to be 105.7 GPa ± 1.6 GPa. Note that for ZIRLO™ modulus measurements, a total number of 200 nano-indents were collected to obtain a representative value for the given loading direction. In addition, the nano-indentation depth was 500 nm, which yields an approximate lateral width of the affected zone of 2.5 micron.

The diffraction elastic constants, \( 1/2S_{11}^{sl} \) and \( S_{11}^{sl} \), for the reflections used for XRD residual stress analysis are given in Table 2.

4.2. Residual stress analysis

For the residual stress determination based on XRD, the 200 reflection was analysed using a standard symmetry geometry as well as an asymmetric diffraction geometry while the other two reflection were analysed using an asymmetric diffraction geometry only. Together with the Rietveld analysis, this gave the residual stress data presented in Table 2 and Fig. 2. Penetration depths (depth that contains 63% of the integrated intensity [21]) for the various reflections and diffraction geometries are also included in Table 2.

The results obtained from the 200 reflection in both diffraction geometries are fairly consistent (−3.9 and −3.4 GPa), differing by about 10% (Fig. 2). The result from the 311 reflection was very similar to the result from the 200 reflection measured in asymmetric geometry. However, the stress analysis based on the 222 reflection alters noticeably, giving −1.6 GPa. The result from the Rietveld analysis, −3.3 GPa, corresponds well with the result obtained from the 311 and 200 reflections.

Fig. 3 displays the shift of the characteristic 249.6 cm⁻¹ Raman peaks and the 684.7 cm⁻¹ peak as a function of stress. In the case of the 249.6 cm⁻¹ peak a linear fit gave a slope of −0.016 and a y-axis intercept of 254.3 cm⁻¹, while the 684.7 cm⁻¹ peak gave a linear fit of −0.034 for the slope and a y-axis intercept of 649.9 cm⁻¹. The amount of Raman peak shift between 0.0% strain to 0.3% strain deformation for the two characteristic peaks were determined to be 2.36 cm⁻¹ (for the characteristic 249.6 cm⁻¹ peak) and 5.11 cm⁻¹ (for the 684.7 cm⁻¹ peak), with corresponding stress increase of 1325 MPa ± 60 MPa.

Therefore the uniaxial piezospectroscopic coefficient for the two TiAlN Raman characteristic peaks were calculated to be: −1.78 cm⁻¹/GPa (for the characteristic 249.6 cm⁻¹ peak) and −3.85 cm⁻¹/GPa (for the 684.7 cm⁻¹ peak).

By implementing Eq. (42), the residual stress obtained in this way is −2.64 GPa (±0.35 GPa) for the 249.6 cm⁻¹ peak and −2.65 GPa (±0.30 GPa) for the 684.7 cm⁻¹ peak.

4.3. Coating fracture stress

The in-SEM loading experiments revealed that the first cracks appear for a corresponding strain of 0.84% ± 0.02%, Fig. 4 (c), resulting in an applied stress of 3.42 GPa ± 0.09 GPa (= \( E_y \cdot \epsilon_y \)). Propagated error was calculated using defined functions according to [27]. The coating fracture strength \( (\sigma_{fracture} = \sigma_{applied stress} + \sigma_{residual stress}) \) is therefore 150 MPa. The error in the fracture strength is discussed further in section 5.2.

With increasing strain, further cracks appeared prior to reaching a saturation state, as shown in Fig. 4 (d), after which little change in crack spacing was evident. The average crack spacing at saturation was measured to be 31 µm ± 7.1 µm.
4.4. Interfacial shear stress (ISS) distribution analysis

Equation (26) shows that the maximum interfacial shear stress (bond strength) is a function of residual stress. Here the Rietveld XRD residual stress value of $3.27 \text{ GPa (±0.12 GPa)}$ was used for interfacial shear strength evaluation. The reason for this choice is given in the discussion. By substituting all the measured or calculated parameters into Equation (26), the maximum interfacial shear stress between the TiAlN and ZIRLO substrate was calculated to be 120 MPa.

Note that the uncertainty of the results was associated in each step of the experimental measurements, but the propagation of errors through calculation were defined using statistical functions [27]. Although the uncertainty in residual stress is thought to be

Table 2
Summary of residual stress results. $1/2S_2^2$ and $S_1$ values for the Rietveld analysis were calculated using bulk modulus and Poisson’s ratio values.

<table>
<thead>
<tr>
<th>Peak</th>
<th>$S_1^{2\text{nd}} \times 10^{-6}$ MPa$^{-1}$</th>
<th>$1/2S_2^{2\text{nd}} \times 10^{-6}$ MPa$^{-1}$</th>
<th>Geometry</th>
<th>Incident angle $\alpha$</th>
<th>Penetration depth $\sin^2 \psi = 0$</th>
<th>Penetration depth $\sin^2 \psi = 0.9$</th>
<th>Residual stress GPa</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>$-0.598$</td>
<td>3.106</td>
<td>Symmetric</td>
<td>0</td>
<td>3.26 $\mu$m</td>
<td>1.03 $\mu$m</td>
<td>$-3.86 \pm 0.04$</td>
</tr>
<tr>
<td>200</td>
<td>$-0.598$</td>
<td>3.106</td>
<td>Asymmetric</td>
<td>10$^\circ$</td>
<td>2.31 $\mu$m</td>
<td>0.73 $\mu$m</td>
<td>$-3.38 \pm 0.08$</td>
</tr>
<tr>
<td>311</td>
<td>$-0.524$</td>
<td>2.882</td>
<td>Asymmetric</td>
<td>10$^\circ$</td>
<td>2.54 $\mu$m</td>
<td>0.80 $\mu$m</td>
<td>$-3.18 \pm 0.18$</td>
</tr>
<tr>
<td>222</td>
<td>$-0.440$</td>
<td>2.631</td>
<td>Asymmetric</td>
<td>10$^\circ$</td>
<td>2.56 $\mu$m</td>
<td>0.81 $\mu$m</td>
<td>$-1.63 \pm 0.08$</td>
</tr>
<tr>
<td>Rietveld</td>
<td>$-0.615$</td>
<td>3.075</td>
<td>Symmetric</td>
<td>0</td>
<td></td>
<td></td>
<td>$-3.27 \pm 0.12$</td>
</tr>
</tbody>
</table>

[Fig. 2. d-spacing v.s. $\sin^2 \psi$ for (a) the 200 peak in symmetric configuration, (b), (c) and (d) for the 200, 311 and 222 peaks respectively in asymmetric configuration, using a 10$^\circ$ incident angle. (e) lattice parameter v.s. $\sin^2 \psi$. Note that the green lines are for intensity and the black lines for the linear fitting of d-spacing v.s. $\sin^2 \psi$. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)]
small in relative terms, it is significant, 120 MPa, in absolute terms, and is also large compared to the interfacial shear strength. The uncertainty in the residual stress value may therefore have quite a large impact on the interfacial shear strength, and the actual value may be significantly higher than 120 MPa.

Using the parameters in Table 3 the distribution of the interfacial shear strength and in-plane stress along a fragment at crack saturation level is plotted, Fig. 5, according to Equation (18) and Equation (17).

5. Discussion

5.1. Residual stress

One of the initial issues encountered in this work was the great variation of residual stresses when using different diffraction peaks or Raman spectroscopy. In metallic materials, the correct choice of reflection is known to be critical for accurate stress analysis by X-ray diffraction since only particular reflections maintain a linear relationship between macroscopic stress and elastic strain in a plastically deformed polycrystalline aggregate. Considering the absence of significant plasticity in TiAlN, one might expect that intergranular strain effects are less of concern here. As two out of the three individually measured reflections agree well with the Rietveld analysis, it might well be the case that the 222 reflection was slightly affected by an underlying Zr substrate reflection. Near surface residual stress profile analysis has been proposed by the use of energy dispersive diffraction taking advantage of the different penetration depth of the various diffraction peaks for such set up [28]. The use of multiple peaks to analyse the residual stress in titanium nitride coatings has also been advocated [29]. Clearly, the present results demonstrate that such an approach is not valid in the case of TiAlN coatings.

It is also interesting to note that previous residual stress analysis of TiAlN coated samples revealed very similar variations with the 200 reflection indicating ~4 GPa while the 111 reflection only suggested stresses in the range of 1.5 GPa [30]. It was explained that this discrepancy might have been the result of diffraction peaks overlapping with those of a different layer in a multi-layer structure.

Rietveld analysis to accurately determine the lattice parameter for residual stress analysis is generally considered to be the most reliable approach as it has been shown to minimise the effect of intergranular strain on stress analysis [31] and relies on a large number of reflections rather than a single peak. Hence, a Rietveld analysis does not only use a single crystallographic grain family but represents more a bulk response of the material. The Rietveld approach also removes the need to use diffraction elastic constants, which can be difficult to obtain (in this work ab-initio single crystal elastic constants were used from literature and converted to diffraction elastic constants). The Raman spectroscopy analysis gave a considerably higher uncertainty compared to the Rietveld analysis. Considering a spot size of about 2 µm, it is also difficult to verify that the positions very near the crack edge are indeed stress free. Considering the high reliability from the Rietveld analysis, it was decided to employ the residual stress value obtained from the Rietveld analysis when calculating the interfacial shear strength.

5.2. Interfacial shear stress (ISS) distribution between TiAlN and ZIRLO substrate

The interfacial shear stress (ISS) and fracture stress are inferred from different experimental measurements to be 120 MPa and 150 MPa from this work. For each separate experiment critical to the ISS calculation, multiple measurements were taken to get statically validate results. The uncertainty in ISS and fracture strength was calculated using the “propagation of uncertainty theory” commonly used in statistical data analysis, where errors were calculated using defined functions detailed in [27]. Both of these values rely on the addition of the applied tensile stress with the compressive residual stress (see Eq. (26)). The uncertainty in both the applied stress and residual stress (90 MPa and 120 MPa respectively), although small in relative terms, are large in absolute terms and especially large in relation to the interfacial shear strength and fracture strength. Therefore, the interfacial shear strength and fracture strength also have large uncertainties associated with them, and are only a best estimate.

The shear-lag model predicts a peak shear stress of ~120 MPa in the vicinity of the fragment ends which may be sufficient to introduce small scale yielding in the substrate. Using the Mises’ yield criterion [32], local yielding would occur if the yield stress of the substrate $\sigma_0$ is given by

$$\sigma_0 < \sqrt{3} \cdot \tau_{\max}$$  \hspace{1cm} (43)

where $\tau_{\max}$ is the maximum interfacial shear strength possible (upper limit). It’s been reported that the yield strength of zirconium alloy (substrate) is approximately 365 MPa [33] suggesting that local yielding of the substrate does not occur according to Equation (43).

It is important to note that a number of researchers have used the Agrawal and Raj (A-R) model which assumes a sinusoidal shear stress rather than one that increases continuously towards the
fragment ends \([8,13]\) as one might expect. For the A-R model the maximum interfacial shear stress (bond strength) is expressed:

\[
\tau_{\text{imax}} = \left( \frac{E_c \cdot \varepsilon_{\text{cf}} + \sigma_f}{1.5} \right) \frac{\pi \cdot \delta}{Z}
\]  

(44)

The A-R model would give an interfacial shear stress estimate (80 MPa), approximately a third smaller than for our approach.

The coating fracture stress is not considerably higher than zero, which suggests that the coating cannot withstand a significant tensile load and fractures almost as soon as the compressive residual stress is overcome by tensile loading. Despite this, the applied tensile stress required to cause fracture is high because of the large compressive residual stress in the coating, which needs to be overcome before the coating can go into tension and fail.

The moderate fracture strength and interfacial shear strength would however have implications if these coatings were to be used in service, as irradiation enhanced creep and irradiation induced

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
<th>Uncertainty</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>TiAlN coating thickness (μm)</td>
<td>8.0</td>
<td>±0.18</td>
<td>Measured</td>
</tr>
<tr>
<td>Steady state crack spacing (μm)</td>
<td>231.0</td>
<td>±7.1</td>
<td>Measured</td>
</tr>
<tr>
<td>Coating bulk modulus Ec (GPa)</td>
<td>406.5</td>
<td>±5.3</td>
<td>Measured</td>
</tr>
<tr>
<td>Substrate modulus Es (GPa)</td>
<td>105.7</td>
<td>±1.6</td>
<td>Measured</td>
</tr>
<tr>
<td>Maximum elastic strain level (%)</td>
<td>0.84</td>
<td>±0.02</td>
<td>Measured</td>
</tr>
<tr>
<td>Residual stress (GPa)</td>
<td>−3.27</td>
<td>±0.12</td>
<td>Measured</td>
</tr>
<tr>
<td>Applied stress (GPa)</td>
<td>3.42</td>
<td>±0.09</td>
<td>Inferred</td>
</tr>
<tr>
<td>Fracture strength (MPa)</td>
<td>150</td>
<td>±150</td>
<td>Inferred</td>
</tr>
<tr>
<td>Interfacial shear strength (MPa)</td>
<td>120</td>
<td>±120</td>
<td>Inferred</td>
</tr>
</tbody>
</table>

Fig. 4. Backscattered electron (BSE) images showing (a) the TiAlN surface before deformation; (b) image obtained at a deformation level of 150 μm; (c) transverse cracks first to appear at a strain level of 0.84%; and (d) cracks at saturation. Note that the features highlighted in the blue boxes were used to calculate the local strain. The transverse cracks in Figure (d) were highlighted as black lines. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 5. Inferred distribution of (a) in-plane coating stress and (b) interfacial shear stress at crack saturation, calculated using the shear-lag model. The horizontal (dashed) line denotes zero stress. Note the length of this predicted crack is the critical crack length when the maximum stress is equal to the fracture stress. Note that the positive and negative signs on the x-axis indicates different directions away from the crack centre.
growth would likely impose a tensile load on the coating. This tensile load may be able to overcome the initial compressive residual stress in the coating and potentially cause coating fracture.

### 6. Limitations

The findings of the current study should be interpreted with caution due to several limitations. The shear-lag model was set-up in a two-dimensional Cartesian coordinate and the whole coating-substrate system was deformed under a uniaxial loading condition. In reality, the cladding is in the form of tubes, i.e., circumferential geometry. The actual deformation mechanism and stress state would be different compared with the results presented in this work. Nevertheless, the calculated interfacial shear strength is useful as an indication of the bond properties, especially for prototype sheet sample products. In addition, the interface was treated as a homogeneous flat region in this work. However, the interface roughness will somewhat influence the load transfer from the substrate to the coating hence affect the interfacial shear strength calculation. Thus, the interfacial shear strength calculated from this study should be considered as an average value of the bond strength rather than a precise measurement of the site-specific interface properties. It is also worth noting that the tests were done at ambient temperature. The performance of the proposed coating at either normal or off-normal service condition is worth investigating, and this is considered in future work.

### 7. Conclusions

A modified shear-lag model has been presented in this paper to estimate the interfacial shear and fracture strength of a TiAlN coating adhered to a ductile ZIRLO™ substrate. The results indicate that during loading of the TiAlN layer transverse cracks, normal to the deformation direction, start to appear at a strain level of 0.84%. With further deformation, more transverse cracks form between existing cracks until a saturation level is reached.

Both Raman and XRD stress measurement show that highly compressive residual stresses remain in the coating after the deposition process. At ambient temperature, soon after the applied stress exceeds the residual stress, cracks start to appear in the TiAlN coating.

The interfacial shear strength between TiAlN and ZIRLO™ substrate has been estimated to be ~120 MPa using the modified shear-lag model, with coating fracture strength of ~150 MPa inferred from the experimentally measured parameters. Hence, the proposed coating candidate demonstrates adequate bonding property. One should note that the coating fails almost as soon as the compressive residual stress is overcome, i.e. most of the apparent strength of the coating comes from the fact that the approximately 3 GPa compressive stress must be overcome before the coating can fail in tension. The moderate fracture strength may have implications if these coatings were used in service, as irradiation enhanced creep and irradiation induced growth would likely impose a tensile load on the coating.

The work demonstrates that X-ray diffraction based residual stress analysis and interfacial shear strength analysis by the combination of multiple techniques can be used in the future to assess bond strength and coating stresses for different manufacturing parameters. It is also planned to use this methodology to determine the evolution of those properties with temperature exposure and autoclave testing.

### Acknowledgements

We would like to acknowledge the support of EPSRC through the project of “Ceramic Coatings for Clad (The C 3 Project): Advanced Accident-Tolerant Ceramic Coatings for Zr-alloy Cladding” (Grants EP/K039237/1). Also this research was funded under a DOE-NEUP Integrated Research Project under contract number 12-4722.