

# Analysis of the transport properties of thermally rearranged (TR) polymers and polymers of intrinsic microporosity (PIM) relative to upper bound performance



Lloyd M. Robeson<sup>a</sup>, Michelle E. Dose<sup>b,\*</sup>, Benny D. Freeman<sup>b</sup>, Donald R. Paul<sup>b</sup>

<sup>a</sup> Department of Materials Science and Engineering, Lehigh University, 1801 Mill Creek Road, Macungie, PA 18062, USA

<sup>b</sup> Department of Chemical Engineering, Texas Materials Institute, Center for Energy and Environmental Research, Center for Research in Water Resources, The University of Texas at Austin, 10100 Burnet Road, Bldg 133, Austin, TX 78758, USA

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## ABSTRACT

A critical analysis comparing the diffusion selectivity, solubility selectivity, diffusivity, and solubility coefficients of thermally rearranged (TR) polymers and polymers of intrinsic microporosity (PIM), two types of polymers which consistently perform at or beyond the polymer upper bound for certain gas pairs (O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>), is reported here. Although most polymers in these two classes exhibit transport properties in the range of typical glassy polymers, several variants offer exceptional performance. The diffusivity selectivity for O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> for TR polymers and PIM lies outside the range of the glassy polymer database. The solubility coefficients for O<sub>2</sub> are at the upper end of the range of both TR and PIM polymers, as is also the case for CO<sub>2</sub> solubility coefficients for PIM polymers. The O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> solubility selectivities for both PIM and TR polymers are in the range of typical glassy polymers. Thus, unique separation values for these polymers are a manifestation of maximizing diffusivity selectivity combined with very high gas solubility. Additionally, the previously determined diffusion gas kinetic diameters,  $d_g$ , were found to correlate best with diffusion coefficients of PIM and TR polymers and serve to better analyze transport properties of upper bound materials.

## 1. Introduction

Polymer membranes were first used for gas phase separations on a commercial scale in the late 1970s by Permea, now Air Products and Chemicals Inc., with the use of their Prism<sup>®</sup> membranes systems for hydrogen recovery from ammonia plant purge streams [1–3]. As of 2016, commercial membrane systems are now employed in many applications, including separation of gas pairs such as O<sub>2</sub>/N<sub>2</sub>, CO<sub>2</sub>/CH<sub>4</sub>, H<sub>2</sub>/N<sub>2</sub>, H<sub>2</sub>/CO<sub>2</sub>, He/air, and H<sub>2</sub>O/natural gas [1–5].

The limits of polymer membrane performance for gas separations has been defined by a relationship termed the “upper bound” [6,7]. The upper bound is an empirical relationship from a log-log plot of ideal permselectivity ( $\alpha_{ij}$ ) versus permeability ( $P_i$ ), where  $i$  represents the more permeable component of the gas pair  $i$  and  $j$ , and  $\alpha_{ij}$  is defined as the ratio of gas pair permeability values ( $P_i/P_j$ ). On these plots, an upper bound line can be drawn above which virtually no data exist, indicating there is a trade-off between permeability and selectivity. In 1999, this empirical relationship was supported by a theoretical prediction of the upper bound parameters by Freeman [6,8]. To delve further into the fundamental properties that lead to this trade-off, the

permeability, diffusivity ( $D$ ), and solubility ( $S$ ) values for a large database of glassy polymers were evaluated. The diffusivity selectivity ( $D_i/D_j$ ) was determined to be the primary factor in establishing the slope of the upper bound, while the solubility selectivity ( $S_i/S_j$ ) had only a modest contribution [9]. Additionally, the gas pair solubility selectivity decreases with increasing free volume and permeability when the diameter of the more permeable gas,  $i$ , is smaller than that of the less permeable gas,  $j$  [9]. Analysis of the diffusion data in glassy polymers yielded a set of gas diameters that were hypothesized to be more relevant for correlating gas diffusion in polymers than prior determinations. In a more recent paper, it was shown that while diffusion coefficients determine the slope of the upper bound, glassy polymers, as opposed to rubbery polymers, tend to dominate the upper bound due to higher solubility coefficient values [10].

Two classes of polymers, in particular, exhibit upper bound properties for many gas pairs and exceed upper bound performance in some cases (e.g., O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>). These groups of polymers are generally referred to as polymers of intrinsic microporosity (PIM) [11–34] and thermally rearranged (TR) polymers [35–44].

PIM were initially investigated by Budd, McKeown and coinvesti-

\* Corresponding author.

E-mail address: [m.dose@utexas.edu](mailto:m.dose@utexas.edu) (M.E. Dose).

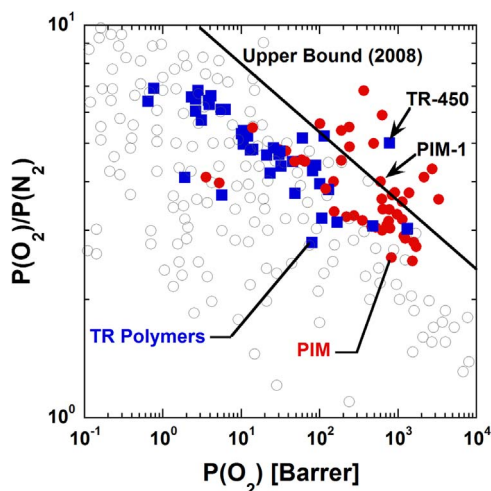
gators at the University of Manchester [11–17,21]. Their synthesis of “ladder” type polymers of intrinsic microporosity (defined as containing interchain spacing or “pores” of < 2 nm) revealed gas separation properties with high gas permeability and upper bound selectivity. The rigid polybenzodioxane backbones of these polymers result in poor molecular packing and thus exhibit high free volume. The upper bound performance of these polymers was attributed to high gas solubility, allowing increased permeability without sacrificing selectivity [15]. This view agrees with the observation that glassy polymers dominate the upper bound, relative to rubbery polymers, due to the dual mode sorption behavior of glassy polymers [10].

Thermally rearranged (TR) polybenzoxazole polymers, initially reported by Lee and coinvestigators, have also generated significant interest for gas separation membranes, specifically for CO<sub>2</sub> based separations [35]. Due to the low solubility of polybenzoxazoles, TR polymers are traditionally formed by the solid state thermal conversion of hydroxyl-containing polyimides to polybenzoxazoles at temperatures ranging from 300 to 450 °C for a prescribed time [45,46]. The exceptional CO<sub>2</sub>/CH<sub>4</sub> selectivity and high permeability of the initial materials were attributed to “well-tuned” cavity formation during thermal rearrangement process. Positron annihilation lifetime spectroscopy (PALS) lent credence to this concept by showing a narrow distribution of the free volume or pore structure after rearrangement.

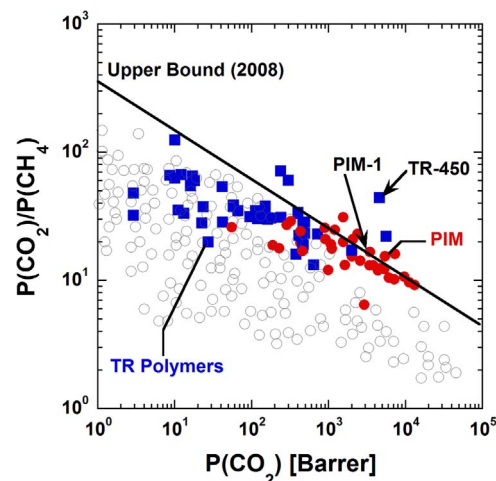
A critical analysis of the diffusion selectivity, solubility selectivity, diffusion coefficients, and solubility coefficients of PIM and TR polymers, as compared with other glassy polymers, is detailed in this paper. A large database of permeability, diffusivity, and solubility data for glassy polymers for the analysis in a previous study was employed in this work [9]. While TR polymers and PIM materials perform at or beyond the upper bound for several different gas pairs, O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> were used for this analysis due to the widespread availability of permeability, solubility, and diffusivity data for O<sub>2</sub>, N<sub>2</sub>, CO<sub>2</sub> and CH<sub>4</sub>, and the lack of necessary data for other gases.

## 2. Analysis of the transport properties of PIM and TR polymers

Permeability data reported for PIM [15,20,22–34] and TR polymers [36,43,44,47–50] are compared for O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> separations in Figs. 1 and 2, respectively. For each case, the data are compared with the appropriate empirical 2008 upper bound [7]. Both PIM and TR polymers have data points above the upper bound



**Fig. 1.** Upper bound relationship for PIM (red circles) and TR polymers (blue squares) for O<sub>2</sub>/N<sub>2</sub> separation. The unfilled circles represent glassy polymers from a previously reported database [9]. The data points for TR-450 [43] and PIM-1 [16] have been highlighted with arrows. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



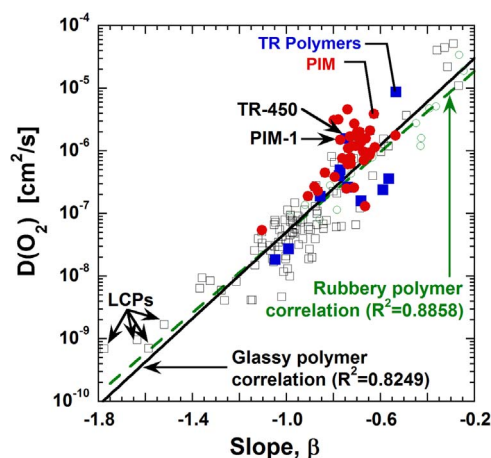
**Fig. 2.** Upper bound relationship for PIM (red circles) and TR polymers (blue squares) for CO<sub>2</sub>/CH<sub>4</sub> separation. The unfilled circles represent glassy polymers from a previously reported database [9]. The data points for TR-450 [43] and PIM-1 [16] have been highlighted with arrows. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

for O<sub>2</sub>/N<sub>2</sub> while predominately TR polymers exceed the upper bound for CO<sub>2</sub>/CH<sub>4</sub>. However, most of the data reported for PIM and TR polymers are close to but below the upper bound relationship, with the exception of a few recently developed PIM materials which significantly exceed the upper bound [27,29,30,32–34]. Some of the PIM variants reported were used to establish the empirical 2008 upper bound [7] and recently, due to the excellent performance of newly developed PIM materials, Swaidan et al. have proposed a new 2015 upper bound for O<sub>2</sub>/N<sub>2</sub> separation [28]. While several TR polymers exceed the 2008 upper bound, TR polymers are not solution-processable and therefore are not formally used to determine the position of the Robeson upper bounds. To serve as reference points, PIM-1 [16] and TR-450 [43] polymers have been highlighted in many of the following figures. PIM-1 is a heavily studied polymer of intrinsic microporosity formed from the condensation of 5,5',6,6'-tetrahydroxy-3,3,3',3'-tetramethyl-1,1'-spirobisindane and tetrafluoroterephthalonitrile. The data used in the remainder of this work is for PIM-1 treated with methanol [16]. TR-450 is the polymer formed from the thermal treatment of a hydroxyl-containing polyimide based off of 2,2-bis(3-amino-4-hydroxyphenyl)-hexafluoropropane (bisAPAF) and 4,4'-hexafluoroisopropylidene diphthalic anhydride (6FDA) moieties, heated at 450 °C for 1 h.

In a previous paper [10], gas diffusion coefficients (*D*) for rubbery and glassy polymers were compared by correlating data sets using the following equation:

$$\ln D = \alpha + \beta d_g^2 \quad (1)$$

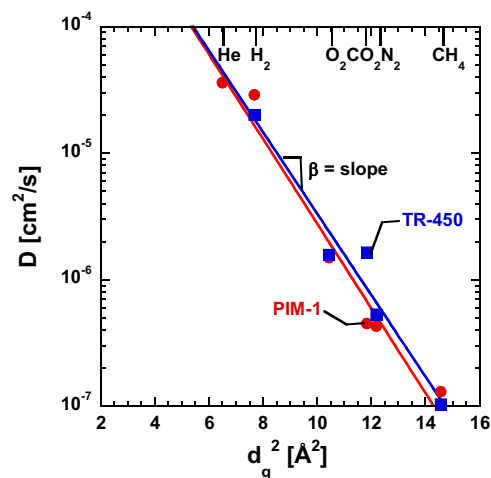
where  $\alpha$  and  $\beta$  are fit for each polymer data set, and  $\beta$  serves as a measure of the size sieving ability of the polymer. The gas diameters,  $d_g$ , were determined in reference [9] by analysis of diffusion in glassy polymers, which provided a prediction of the gas diameters of He, H<sub>2</sub>, O<sub>2</sub>, N<sub>2</sub>, and CO<sub>2</sub> once the diameter of CH<sub>4</sub> was fixed. By plotting the diffusion coefficients for a gas of intermediate diameter (O<sub>2</sub>,  $d_g = 3.23$  Å) as a function of the slope,  $\beta$ , as defined by Eq. (1), considerable overlap in the data for glassy and rubbery polymers suggested only modest differences in the diffusion selectivity between the two different polymer classes [10]. This deeper analysis of diffusion coefficients contradicted previous beliefs that glassy polymers dominated the upper bound due to higher diffusivity selectivity than rubbery polymers [9,10]. This analysis has been extended to this study, as shown in Fig. 3. Additional data have been added to the previous analysis [10], where diffusion values of at least 5 of the 6 mentioned gases have been reported [51–61]. Values for PIM [15,22–33], TR



**Fig. 3.** Correlation of glassy (black unfilled squares) and rubbery (green unfilled circles) polymer data for oxygen diffusion coefficients ( $d_g = 3.25 \text{ \AA}$ ) from Eq. (1) [10], with PIM (red circles) and TR polymers (blue squares) highlighted to indicate agreement with previous analysis. Liquid crystalline polymers (LCPs), TR-450, and PIM-1 are indicated by arrows. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

polymers [36,43,44], and liquid crystalline polymers (LCPs) [51,61,62] have also been included to provide a comparison for gas diffusivity in polymers with high and very low permeabilities. Each point on the plot represents a polymer from the indicated data set. As in the previous paper, the glassy and rubbery polymer correlation lines are quite similar [10]. Thus, the diffusion selectivity of glassy and rubbery polymers are not as different as once believed, even for upper bound materials such as PIM and TR polymers. The data points for TR-450 and PIM-1, highlighted in Fig. 3, lie above the glassy polymer correlation. Thus, both families of materials have diffusion coefficients significantly higher than other polymers of similar  $\beta$  value (i.e., similar size sieving ability). For this reason, PIM-1 [16] and TR-450 [43] have been selected to represent the PIM and TR polymer data sets. Liquid crystalline polymers also exhibit higher diffusion coefficients versus the correlation line at the lower end of the permeability range.

Fig. 4 presents a comparison of diffusion coefficients for TR-450 and PIM-1 versus gas diameter. The gas diameter values utilized for this figure were those noted for Fig. 3 and reported in reference [10]. As predicted by Eq. (1), the diffusion coefficients follow a linear correlation with gas diameter squared, and there is no discernible



**Fig. 4.** Diffusion coefficients versus gas diameter squared ( $d_g^2$ ) for PIM-1 (red circles) and TR-450 (blue squares). The specific expressions of Eq. (1) for TR-450 [43]. The parameters for the shown linear fits to Eq. (1) are included in Table 1. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

**Table 1**

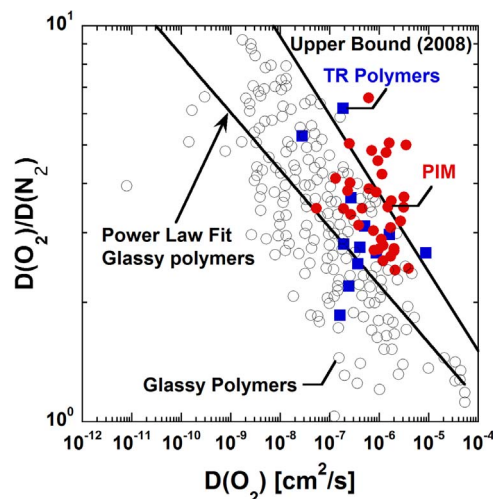
Parameters for Eq. (1) used to correlate diffusion coefficients ( $\text{cm}^2/\text{s}$ ) for PIM-1 and TR-450 versus the gas diffusion diameters,  $d_g$  ( $\text{\AA}$ ). The parameters and uncertainties were determined assuming a 10% uncertainty in the diffusion coefficient values and a least square fit analysis.

Material	$\alpha$	$\beta$	$R^2$
PIM-1	$-5.3 \pm 0.2$	$-0.75 \pm 0.01$	0.968
TR-450	$-5.2 \pm 0.2$	$-0.74 \pm 0.02$	0.955

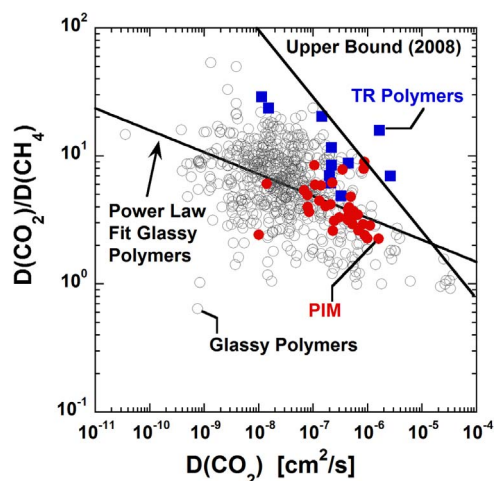
difference between the trends for PIM-1 and TR-450. The parameters fitting Eq. (1) to PIM-1 and TR-450 diffusion coefficients are included in Table 1. These results agree with previous observations [9] that the dependence of gas diffusion coefficients on the square of gas diameters (i.e.,  $\beta$  in Eq. (1)) is similar when polymers have similar diffusion coefficients. Interestingly, the diffusion coefficient of  $\text{CO}_2$  ( $d_g^2 = 11.8 \text{ \AA}^2$ ) in TR-450 lies significantly above the linear correlation. This deviation may contribute to the fact that TR-450 exceeds the 2008 upper bound properties for  $\text{CO}_2/\text{CH}_4$  separation (cf., Fig. 2) [7].

PIM and TR polymers are often reported to have transport properties near or above the upper bound for the  $\text{O}_2/\text{N}_2$  and  $\text{CO}_2/\text{CH}_4$  gas pairs. The diffusivity selectivity for PIM and TR polymers are compared to the rest of the glassy polymer database in Figs. 5 and 6 for  $\text{O}_2/\text{N}_2$  and  $\text{CO}_2/\text{CH}_4$ , respectively. As expected, the glassy polymer data show a distinct upper bound relationship for both gas pairs in log-log plots of diffusivity selectivity ( $D_i/D_j$ ) versus diffusivity of the faster component ( $D_i$ ). Similar to the permeability upper bound (cf., Fig. 1), several PIM and TR polymers lie on or above the diffusivity upper bound for  $\text{O}_2/\text{N}_2$ . For  $\text{CO}_2/\text{CH}_4$  separation, several TR polymers show equal or higher diffusivity selectivity than the glassy polymer diffusivity upper bound, while PIM have properties comparable to those of other glassy polymers. Power law fits for  $D_i/D_j$  with respect to  $D_i$  (i.e.,  $\log\left(\frac{D_i}{D_j}\right) = A \log(D_i) + B$ ) have been included for all data points in Figs. 5 and 6 to show the general trend of decreasing diffusion selectivity with increasing diffusivity.

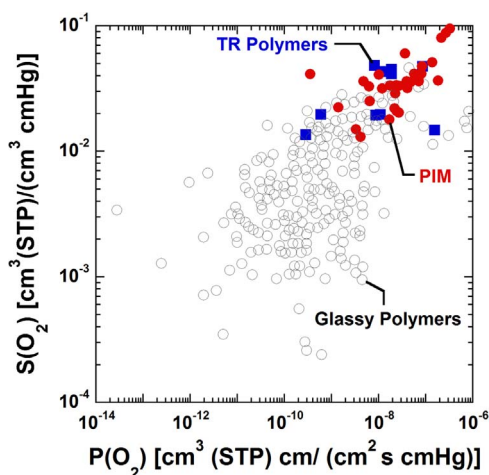
The solubility data for PIM [11–34] and TR polymers [35–44] were obtained from the references noted earlier. A plot of solubility constants versus permeability coefficients is shown for  $\text{O}_2$  solubility (Fig. 7) and  $\text{CO}_2$  solubility (Fig. 8). These data are compared with similar data for other glassy polymers from reference [9]. All data shown fall within the trend noted previously [9], where the solubility coefficients generally increase with increasing permeability. However,



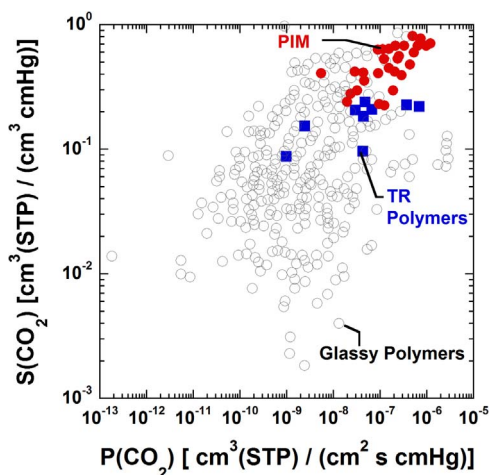
**Fig. 5.** Diffusivity upper bound correlation for  $\text{O}_2/\text{N}_2$ , comparing PIM (red circles) and TR polymers (blue squares) to the glassy polymer database (unfilled circles) [9]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 6.** Diffusivity upper bound correlation for  $\text{CO}_2/\text{CH}_4$ , comparing PIM (red circles) and TR polymers (blue squares) to the glassy polymer database (unfilled circles) [9]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 7.** Comparison of  $\text{O}_2$  solubility coefficient data of PIM (red circles) and TR variants (blue squares) with the glassy polymer database (unfilled circles) [9]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 8.** Comparison of  $\text{CO}_2$  solubility coefficient data of PIM (red circles) and TR polymers (blue squares) with the glassy polymer database (unfilled circles) [9]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

**Table 2**

$\text{O}_2/\text{N}_2$  and  $\text{CO}_2/\text{CH}_4$  gas pair selectivity values for glassy polymers, PIM, and TR polymers. The indicated references denote which data sets were used to obtain the average value and range shown.

Polymer	$S(\text{O}_2)/S(\text{N}_2)$		$S(\text{CO}_2)/S(\text{CH}_4)$	
	Average	Range	Average	Range
glassy polymers[9]	1.30	0.31–2.50	5.00	0.93–47.5
PIM[15,22–24]	1.16	1.03–1.44	4.35	3.19–5.09
TR polymers[36,43,44]	1.39	1.05–1.83	3.02	2.50–4.30

both PIM and TR polymers show  $\text{O}_2$  solubility values towards the higher end of the trend. Additionally, PIM materials exhibit higher  $\text{CO}_2$  solubility coefficients relative to the spread of the data for glassy polymers, while TR polymers have values scattered within the glassy polymer data set. Compared to other glassy polymers, TR polymers and PIM have both high solubility and diffusivity coefficients. These “upper limit” transport properties contribute significantly to the upper bound behavior of these two polymer classes.

The gas pair selectivities ( $S_i/S_j$ ) were calculated for PIM and TR polymers. The results are summarized in Table 2, where the average and range of solubility selectivity values are reported. These results indicate both PIM and TR polymers have solubility selectivities within the general range of glassy polymers. This supports the previous analysis that high solubility, rather than solubility selectivity, contributes to polymers dominating upper bound behavior.

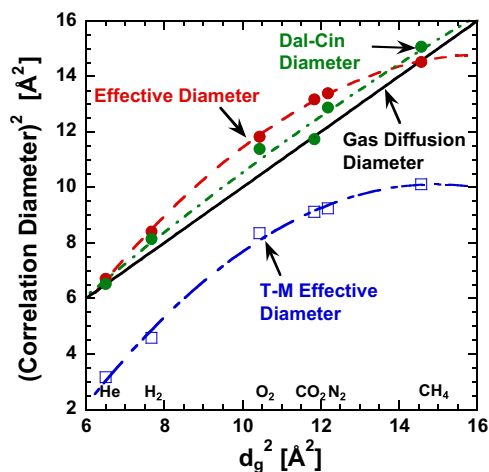
### 3. Correlation of PIM and TR polymer diffusion data with gas diameter

Correlations of gas diffusion coefficients in polymers with gas molecular dimensions (i.e., diameter squared or gas molecule volume) have been often reported in the literature. Grün, and several others since, have correlated diffusion coefficients with van der Waals molecular volume for a variety of gas permeants, ranging from He to n-hexane, in both polymers and solvents [63,64]. However, for small molecules, this correlation tends to be weak due to the non-spherical nature of gas molecules like  $\text{H}_2$ ,  $\text{O}_2$ ,  $\text{N}_2$ , and  $\text{CO}_2$ . For this reason, several prominent correlations relating diffusion coefficients to the gas kinetic diameter exist. These include: the kinetic diameter determined from zeolite data (Breck diameters) [65], the Lennard-Jones gas diameter and collision diameter [66,67], the effective diameter [59], the Dal-Cin correlation diameter from analysis of the upper bound [68], the permeability correlation diameter [69], the Teplyakov-Mears (T-M) diameter [70], and the diffusion correlation diameter determined from glassy polymer data [9]. The Teplyakov-Mears (T-M) diameter correlation comprises a comprehensive list of gas diameters based on analysis of noble gas diffusion in a series of polymers to yield a fit to Eq. (1). While several of these correlations use the diameter of methane (a relatively spherical molecule) as a reference point, the T-M correlation used noble gases [70]. This choice resulted in diameters significantly lower than the other noted correlations (cf., Table 3). While the absolute values of the T-M diameters are lower, the correlation ability to fit the gas diffusion data to the relative difference in the diameter squared is the key factor, not the magnitude of the gas diameter values. A comparison of the gas diameters utilized to correlate diffusion data is shown in Table 3.

The literature database for glassy [9] and rubbery polymers [10] yields the following relationship for diffusion coefficients:  $D(\text{He}) > D(\text{H}_2) > D(\text{O}_2) > D(\text{CO}_2) > D(\text{N}_2) > D(\text{CH}_4)$ . The closest proximity for the gas pairs is with  $D(\text{CO}_2)$  and  $D(\text{N}_2)$ , with  $D(\text{CO}_2)$  only slightly higher than  $D(\text{N}_2)$ . Four of the noted gas diameter correlations show this trend with the diameter of  $\text{CO}_2$  being only slightly smaller than  $\text{N}_2$ . These include the T-M diameter, effective diameter, Dal-Cin correlation diameter, and the diffusion correlation diameter. While the perme-

**Table 3**  
Gas diameters determined by different methods reported in the literature.

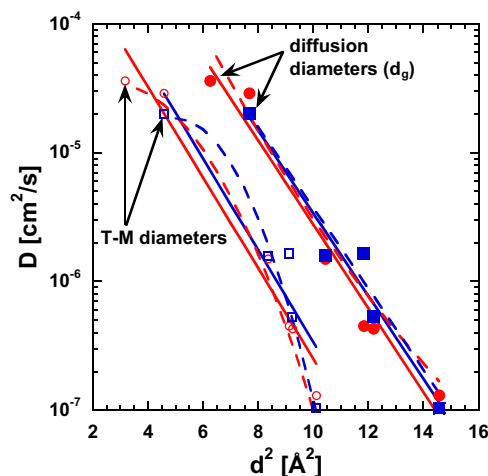
Gas	Gas Diameter (Å)				Permeability[69]	Breck[65]	Effective[59]	Diffusion, $d_g$ [9]
	Teplyakov-Mearns (T-M) [70]	Lennard-Jones[67]	Dal-Cin[68]	Lennard-Jones Collision[66]				
He	1.78	2.551	2.555	2.576	2.644	2.6	2.59	2.55
H <sub>2</sub>	2.14	2.827	2.854	2.915	2.875	2.89	2.90	2.77
O <sub>2</sub>	2.89	3.467	3.374	3.433	3.347	3.46	3.44	3.23
CO <sub>2</sub>	3.02	3.941	3.427	3.996	3.325	3.3	3.63	3.44
N <sub>2</sub>	3.04	3.798	3.588	3.681	3.568	3.64	3.66	3.49
CH <sub>4</sub>	3.18	3.758	3.882	3.822	3.817	3.8	3.81	3.817



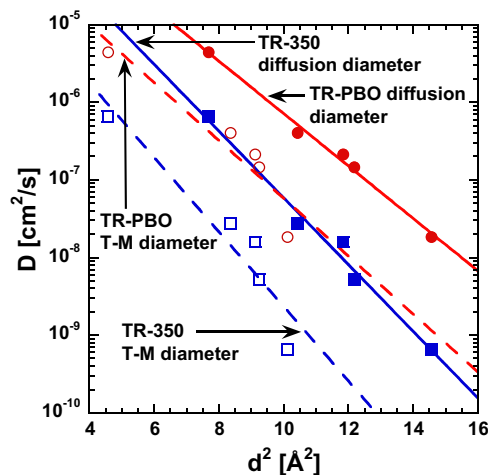
**Fig. 9.** Comparison of the effective [59], Dal-Cin [68], and Teplyakov-Mearns [70] diameter correlations to the gas diffusion correlation diameter squared ( $d_g^2$ ) [9]. A parity line (the solid, straight line) for the gas diffusion correlation diameter has been included as a reference.

ability [69] and Breck [65] correlations give the diameters for CO<sub>2</sub> and N<sub>2</sub> in the appropriate size order, the differences are too large to reflect the small observed difference in diffusion coefficients. A comparison of these diameters (squared) plotted against the diffusion correlation diameter ( $d_g$ ) is shown in Fig. 9 with a polynomial fit of the data. The comparison illustrated in Fig. 9 shows convex behavior for the effective diameter and the T-M diameter relative to the diffusion correlation diameter (all squared). The Dal-Cin diameter is quite close to linearity but shows a slight deviation for CO<sub>2</sub>.

A comparison of the diffusion correlation diameter and the T-M diameter is presented in Fig. 10 with diffusion coefficient data for PIM-1 and TR-450. A linear fit of the data as well as a quadratic fit are shown, and a statistical assessment of these fits has been performed in the Supporting Information. Good linearity, as predicted by Eq. (1), is observed for the diffusion correlation diameter data, whereas convex behavior is observed for the T-M diameter. The linear behavior is also observed with several other TR polymers as shown in Fig. 11. While the TR and PIM polymers better obey correlations with the diffusion correlation diameters, the T-M diameters often yield a better fit, as compared to  $d_g$ , with typical rubbery and non-upper bound glassy polymers. The gas diffusion correlation diameter (based only on glassy polymer data) often yields modestly concave behavior for  $\ln(D)$  versus  $d_g^2$  plots for rubbery and non-upper bound glassy polymers. The better fit of the TR and PIM diffusivities with the diffusion correlation diameters than with diameters from other correlations appears to be a consequence of the larger relative gas diameter difference between O<sub>2</sub>, N<sub>2</sub>, and CH<sub>4</sub> in  $d_g$  than in the other correlations.



**Fig. 10.** Comparison of the fit of Eq. (1) for PIM-1 (red circles) [16] and TR-450 (blue squares) [43] employing the T-M diameters (unfilled markers) and the diffusion correlation diameters (filled markers). A linear fit (solid line) and a quadratic fit (dashed line) are shown for each correlation. The linear and quadratic fit parameters are listed in Table S1.



**Fig. 11.** Comparison of TR-PBO (red circles) and TR-350 (blue squares) diffusion data [43] fit with Eq. (1) employing the T-M diameters (open markers) and the diffusion correlation diameters (filled markers). Linear correlations for each data set are included. TR-350 is a TR polymer treated at 350 °C for 1 h for partial conversion to the PBO structure, and TR-PBO is a polymer treated at 450 °C for 1 h to achieve 100% conversion to the PBO structure [43]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

#### 4. Conclusions

The transport properties of PIM and TR polymers variants have been compared with the spread of data for glassy polymers [71]. The diffusivity selectivity of common gases for specific TR and PIM variants

is modestly higher than most glassy polymers. For specific gas pairs (i.e., O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>), some TR and PIM variants also offer higher diffusivity selectivity than other glassy polymers when compared on a diffusivity selectivity upper bound plot (i.e., log(D<sub>i</sub>/D<sub>j</sub>) versus D<sub>i</sub>), although most of the variants are in the range of other glassy polymers. The natural log diffusion coefficient versus gas diameter squared correlations (i.e., Eq. (1)) is best fit by the diffusion correlation diameters, d<sub>g</sub>, than by various other gas diameter correlations commonly employed for polymers.

The solubility coefficients of PIM variants for O<sub>2</sub> and CO<sub>2</sub> are in the higher range of the spread of glassy polymer data. TR variants show higher O<sub>2</sub> solubility coefficients relative to other glassy polymers but have CO<sub>2</sub> solubility coefficients more in the range of other glassy polymers. The O<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> solubility selectivities for both PIM and TR variants are in the expected range for glassy polymers.

The basic conclusion from this analysis is that the upper bound performance (i.e., combination of high permeability and permeability selectivity) for specific PIM and TR polymers is due to a combination of higher diffusion selectivity, high diffusion coefficients, and high solubility coefficients, relative to other glassy polymers. The high solubility coefficients are a consequence of high free volume combined with high glass transition temperatures, leading to significant dual mode sorption, as noted previously [9]. Elevated solubility shifts the data to higher permeability values relative to other polymers at a given selectivity on the upper bound plots. This point has been recognized in an earlier hypothesis on PIM variants [15] and further supported by the evidence presented in this study. Thus, the excellent performance of TR and PIM variants is a consequence of maximizing diffusion selectivity, diffusion coefficients, and gas solubility. They appear to fit the solution-diffusion model and are not uniquely different in their transport mechanism than other polymers. Thus, upper bound behavior can be achieved when diffusion selectivity, diffusion coefficients, and gas solubility are simultaneously maximized.

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## Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at doi:10.1016/j.memsci.2016.11.085.

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